

AMS PREVIOUS YEAR QUESTIONS SET

1. Find $\frac{dy}{dx}$ if $y = e^x \cdot \sin x$ (2marks)
2. Evaluate $\int \cos^2 x \, dx$ (2marks)
3. Evaluate $\int \frac{1}{3x+7} \, dx$ (2 marks)
4. Find $\frac{dy}{dx}$ if $y = \log(xe^x)$ (4marks)
5. Evaluate $\int \frac{\cos \sqrt{x}}{\sqrt{x}} \, dx$ (4marks)
6. Evaluate $\int \frac{1}{x^2 + 3x + 2} \, dx$ (4 marks)
7. Evaluate $\int \frac{1}{5+4\cos x} \, dx$ (4 marks)
8. Evaluate $\int \frac{1-\tan x}{1+\tan x} \, dx$ (4 marks)
9. Evaluate $\int \frac{\log x}{x(\log x+2)(\log x+3)} \, dx$ (4marks)
10. Evaluate $\int_0^7 \frac{\sqrt[3]{x}}{\sqrt[3]{x} + \sqrt[3]{7-x}} \, dx$ (4marks)
11. Find the area of circle by using definite integration $x^2 + y^2 = 25$ (6 marks)
12. Find the order and the degree of differential equation $\frac{d^2y}{dx^2} = [1 + (\frac{dy}{dx})^2]^{\frac{3}{2}}$ (3marks)
13. Solve differential equation $x\sqrt{1-y^2}dx + y\sqrt{1-x^2}dy = 0$ (3 marks)
14. The velocity of particle is given by $V = t^2 - 6t + 7$ find the distance covered in 3 seconds (3 marks)
15. Find $\frac{dy}{dx}$ if $x \sin y + y \sin x = 0$ (2marks)
16. Find $\frac{dy}{dx}$ if $y = a^x + x^a + a^a + \sqrt{x}$ (2 marks)
17. Evaluate $\int \frac{1}{x^2 + 4} \, dx$ (2 marks)
18. Evaluate $\int x e^x \, dx$ (2 marks)
19. Evaluate $\int \frac{(x-1)e^x}{x^2 \sin^2 \frac{e^x}{x}} \, dx$ (4 marks)
20. Evaluate $\int \frac{dx}{4\cos^2 x + 9\sin^2 x}$ (4 marks)
21. Evaluate $\int \frac{\log x}{x[2+\log x][3+\log x]} \, dx$ (4 marks)
22. Evaluate $\int x \cdot \tan^{-1} x \, dx$ (4marks)
23. Evaluate $\int \frac{x}{(x+1)(x+2)} \, dx$ (4 marks)
24. Evaluate $\int_2^5 \frac{\sqrt{x}}{\sqrt{7-x} + \sqrt{x}} \, dx$ (4 marks)
25. Verify that $y = \log x$ is a solution of differential equation $x \frac{d^2y}{dx^2} + \frac{dy}{dx} = 0$ (3 marks)
26. The velocity of particle is given by $v = t^2 - 6t + 7$ find the distance covered in 3 sec initially $x=0$ when $t=0$ (3 marks)
27. Solve $(1+x^2)dy - (1+y^2)dx = 0$ (3marks)
28. Solve $\frac{dy}{dx} + y \cot x = \cos x$ (3 marks)

$$29. \text{Evaluate } \int x(x-1)^2 dx$$

$$30. \text{Evaluate } \int \sin^2 2x dx$$

$$31. \text{Find } \frac{dy}{dx} \text{ if } y = e^x \sin^{-1} x$$

$$32. \text{If } 13x^2 + 2x^2y + y^3 = 1 \text{ find } \frac{dy}{dx} \text{ at } (1, -2)$$

$$33. \text{If } x=a(\theta + \sin \theta), y=a(1 - \cos \theta) \text{ find } \frac{dy}{dx} \text{ at } \theta = \frac{\pi}{2}$$

$$34. \text{Evaluate } \int x \sin^{-1} x / \sqrt{1-x^2} dx$$

$$35. \text{Evaluate } \int \frac{\cos x}{1+\sin^2 x} dx$$

$$36. \text{Evaluate } \int \frac{dx}{3-2\sin x}$$

$$37. \text{Evaluate } \int \frac{\log x}{x(2+\log x)(3+\log x)} dx$$

$$38. \text{Find } \frac{dy}{dx} \text{ if } y = \log \left(\frac{\sin x}{1+\cos x} \right)$$

$$39. \text{Evaluate } \int \frac{x+1}{x^2(x-2)} dx$$

$$40. \int \frac{\sqrt[3]{x+5}}{\sqrt[3]{x+5} + \sqrt[3]{9-x}} dx$$

$$41. \text{Find the order and degree of differential equation } \frac{d^2y}{dx^2} = \left(y + \frac{dy}{dx} \right)^{\frac{3}{2}}$$

$$42. \text{solve } x \frac{dy}{dx} - y = x^2$$

$$43. \text{Evaluate } \int \frac{1}{\sin^2 x \cdot \cos^2 x} dx$$

$$44. \text{Evaluate } (1+\sqrt{x})^2 / \sqrt{x} dx$$

$$45. \text{Find } \frac{dy}{dx} \text{ if } x^2 + y^2 = xy$$

$$46. \text{If } x=3\sin 4\theta, y=4\cos 3\theta \text{ Find } \frac{dy}{dx}$$

$$47. \text{If } y=\log (\sec x + \tan x) \text{ find } \frac{dy}{dx}$$

$$48. \text{Find } \frac{dy}{dx} \text{ if } y = x^x + (\cos x)^x$$

$$49. \text{Evaluate } \int_0^{\frac{\pi}{2}} \frac{1}{1+\cot x} dx$$

$$50. \text{Evaluate } \int \frac{dx}{2+3\cos x}$$

$$51. \text{Evaluate } \int \frac{1}{\sqrt{3-x-x^2}} dx$$

$$52. \text{Evaluate } \int \frac{x}{x^2+3x-4} dx$$

$$53. \text{Solve } (x+1) \frac{dy}{dx} - y = e^x (x+1)^2$$

$$54. \text{Find the value of } a \text{ if } f(x) = ax + 10 \text{ and } f(1) = 13$$

$$55. \text{Find } \frac{dy}{dx} \text{ if } y = x^e + e^x + e^e + \sqrt{x}$$

$$56. \text{Evaluate } \int e^x + x^e + e^e dx$$

$$57. \text{Evaluate } \int \frac{\cos(\log x)}{x} dx$$

$$58. \text{Find } \frac{dy}{dx} \text{ if } x^3 + y^3 + xy = 0$$

